

Q 1	mark	Sub	
(a) (i) (A) PCLM $\rightarrow +ve$ $2 \times 4 - 6 \times 2 = 8v$  $v = -0.5$ so $0.5 \text{ m s}^{-1}$ in opposite direction to initial motion of P	M1 A1 A1	Use of PCLM and correct mass on RHS Any form Direction must be negative and consistent or clear. Accept use of a diagram.	3
(B)  $0.5 \times 2 \times 4^2 + 0.5 \times 6 \times 2^2 - 0.5 \times 8 \times (-0.5)^2$  $= 27 \text{ J}$	M1 A1	Use of KE. Must sum initial terms. Must have correct masses FT <b>their</b> (A) only	2
(ii) (A) PCLM $\rightarrow +ve$ $2 \times 4 - 6 \times 2 = 2v_p + 6v_Q$ $v_p + 3v_Q = -2$ NEL $\rightarrow +ve$ $\frac{v_Q - v_p}{-2 - 4} = -\frac{2}{3}$ $v_Q - v_p = 4$ $v_Q = 0.5$ so $0.5 \text{ m s}^{-1}$ in orig direction of P $v_p = -3.5$ so $3.5 \text{ m s}^{-1}$ in opp to orig dir of P	M1 A1  M1 A1 A1 A1	Use of PCLM Any form  NEL Any form cao. Direction need not be made clear. cao. Direction must be negative and consistent or clear (e.g diag)	6
(B)  $\rightarrow +ve$ $2 \times -3.5 - 2 \times 4 = -15 \text{ N s}$ so $15 \text{ N s}$ in opp to orig direction	M1 A1	Use of change in momentum with correct mass. FT (A). Dir must be clear (e.g. diag)	2
(b)  Let $\alpha = \arcsin(12/13)$ and $\beta = \arcsin(3/5)$ Parallel: $26 \cos \alpha = u \cos \beta$  so $26 \times \frac{5}{13} = u \times \frac{4}{5}$ and $u = 12.5$  Perp: $e = \frac{u \sin \beta}{26 \sin \alpha}$  $\frac{12.5 \times \frac{3}{5}}{26 \times \frac{12}{13}} = \frac{5}{16}$	M1 A1 A1  M1 F1  F1	PCLM parallel to plane attempted. At least one resolution correct    NEL on normal components attempted. FT <b>their</b> $u$  FT <b>their</b> $u$	6
			19

Q 2	mark	Sub	
(i) Diagrams  cw moments about A $2 \times 90 - 3R_B = 0$ $R_B = 60$ so 60 N upwards  cw moments about R: $T \downarrow$ $75 \times 1 + 3T - 60 \times 0.5 = 0$  $T = -15$ so 15 N upwards	B1  M1 A1  M1 A1 A1	Internal force at B must be shown  1 <sup>st</sup> moments equation attempted for either force. Accept direction not specified  2 <sup>nd</sup> moments equation for other force. All forces present. No extra forces. Allow only sign errors Direction must be clear (accept diag)	6
(ii) cw moments about A $90 \times 2 \cos 30 - V \times 3 \cos 30 - U \times 3 \cos 60 = 0$  giving $60\sqrt{3} = U + V\sqrt{3}$	M1 A1 E1	Moments equation with resolution. Accept terms missing All correct. Allow only sign errors. Clearly shown	3
(iii) Diagram	B1	$U$ and $V$ correct with labels and arrows	1
(iv) ac moments about C $75 \times 2 \cos 30 + 3.5V \cos 30 - 3.5U \cos 60 = 0$  $\frac{300}{7}\sqrt{3} = U - V\sqrt{3}$  Solving for $U$ and $V$ $U = \frac{360\sqrt{3}}{7}$ (= 89.0768...) $V = \frac{60}{7}$ (= 8.571428...)  Resolve $\rightarrow$ on BC $F = U$ so frictional force is $\frac{360\sqrt{3}}{7}$ N (= 89.1 N (3 s. f.))	M1 B1 A1  M1 A1 F1  M1 F1	Moments equation with resolution. Accept term missing At least two terms correct (condone wrong signs) Accept any form  Any method to eliminate one variable Accept any form and any reasonable accuracy Accept any form and any reasonable accuracy [Either of $U$ and $V$ is cao. FT the other]	8
			18

Q 3	mark	Sub	
(a)	$20000 = (R + 900g \times 0.1) \times 16$ $R = 368 \text{ so } 368 \text{ N}$	M1 Use of $P = Fv$ , may be implied. B1 Correct weight term A1 All correct A1	4
(b) (i)	$F_{\max} = \mu mg \cos \alpha$ <p>Force down slope is weight cpt <math>mg \sin \alpha</math></p> <p>Require <math>\mu mg \cos \alpha \geq mg \sin \alpha</math></p> <p>so <math>\mu \geq \tan \alpha = \frac{5}{12}</math></p>	B1 Correct expression for $F_{\max}$ <b>or</b> wt cpt down slope (may be implied and in any form) B1 Identifying $\sin \alpha$ as $\frac{5}{13}$ or equivalent E1 Proper use of $F \leq \mu R$ or equivalent. [ $\mu = \tan \alpha$ used WW; SC1]	3
(ii)	<p><b>either</b></p> $0.5 \times 11 \times v^2$ $= 11g \times 1.5 \times \frac{5}{13} + 0.2 \times 11g \times 1.5 \times \frac{12}{13} + 9$ $v^2 = 18.3717\dots$ $v = 4.2862\dots \text{ so } 4.29 \text{ m s}^{-1} \text{ (3 s. f.)}$ <p><b>or</b></p> <p>+ ve up the slope</p> $-11g \times \frac{5}{13} - 0.2 \times 11g \times \frac{12}{13} - 6 = 11a$ $a = -6.1239 \text{ m s}^{-2}$ $v^2 = -3a$ $v = 4.286 \text{ m s}^{-1}$	M1 Use of work energy with at least three required terms attempted B1 Any term RHS. Condone sign error. B1 Another term RHS. Condone sign error. A1 All correct . Allow if trig consistent but wrong A1 cao M1 Use of N2L B1 Any correct term on LHS A1 M1 use of appropriate $uvast$ A1 c.a.o.	5
(iii)	<b>continued overleaf</b>		

4762

Mark Scheme

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<p><b>3</b></p> <p>(iii) <b>continued</b></p> <p><b>either</b>          Extra GPE balances WD against resistances  <math>mgx \sin \alpha</math>  <math>= 6(x+3) + 0.2 \times 11g \times \cos \alpha (x+3)</math></p> <p><math>x = 4.99386\dots</math> so 4.99 m (3 s. f.)</p> <p><b>or</b>  <math>0.5 \times 11 \times 18.3717\dots</math>  <math>= (1.5+x) \times 11g \times \frac{5}{13} - 6(1.5+x)</math>  <math>-(1.5+x) \times 0.2 \times 11g \times \frac{12}{13}</math></p> <p><math>x = 4.99386\dots</math> so 4.99 m (3 s. f.)</p> <p><b>or</b>          + ve down the slope  <math>11g \times \frac{5}{13} - 0.2 \times 11g \times \frac{12}{13} - 6 = 11a</math></p> <p><math>a = 1.4145\dots \text{ m s}^{-2}</math>  <math>4.286^2 = 2a(1.5+x)</math></p> <p><math>x = 4.99</math></p>		<p>M1 Or equivalent</p> <p>B1</p> <p>B1 One of 1<sup>st</sup> three terms on RHS correct</p> <p>B1 Another of 1<sup>st</sup> 3 terms on RHS correct</p> <p>A1 All correct. FT <b>their</b> v if used.</p> <p>A1 cao.</p> <p>M1 Allow 1 term missing</p> <p>B1 KE. FT <b>their</b> v</p> <p>B1 Use of 1.5 + x (may be below)</p> <p>B1 WD against friction</p> <p>A1 All correct</p> <p>A1 cao.</p> <p>M1 N2L with all terms present</p> <p>A1 all correct except condone sign errors</p> <p><b>A1</b></p> <p><b>M1</b> use of appropriate <i>uvast</i></p> <p><b>B1</b> for (1.5 + x) (may be implied)</p> <p>A1 c.a.o.</p>	<p>6</p>
			18

Q 4	mark	Sub
(i) $100 \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = 10 \begin{pmatrix} 5 \\ 0 \end{pmatrix} + 30 \begin{pmatrix} 10 \\ 15 \end{pmatrix} + 30 \begin{pmatrix} 20 \\ 15 \end{pmatrix} + 30 \begin{pmatrix} 25 \\ 30 \end{pmatrix}$  $100 \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = \begin{pmatrix} 1700 \\ 1800 \end{pmatrix}$ $\bar{x} = 17$ $\bar{y} = 18$	M1 Correct method for c.m.  B1 Total mass correct B1 One c.m. on RHS correct [If separate components considered, B1 for 2 correct]  A1 cao A1 cao. [Allow SC 4/5 for $\bar{x} = 18$ and $\bar{y} = 17$ ]	5
(ii) (17,18,20)	B1 x- and y- coordinates. FT from (i). B1 z coordinate	2
(iii) cw moments about horizontal edge thro' D x component $P \times 20 - 60 \times (20 - 17) = 0$  $P = 9$	M1 Or equivalent with all forces present  B1 One moment correct (accept use of mass or length) B1 correct use of <b>their</b> $\bar{x}$ in a distance A1 FT only <b>their</b> $\bar{x}$	4
(iv) Diagram	B1 Normal reaction must be indicated acting vertically upwards at edge on Oz and weight be in approximately the correct place.	1
(v) On point of toppling ac moments about edge along Oz $30 \times Q - 60 \times 17 = 0$  $Q = 34$ Resolving horizontally $F = Q$ As $34 > 30$ , slips first	M1 Or equivalent with all forces present B1 Any moment correct (accept use of mass or length) F1 FT only <b>their</b> $\bar{x}$ B1 B1 FT <b>their</b> Q correctly argued.	5
		17